GSI-RRTF: follow-up meeting on Open HF transport coefficients **Nonperturbative Open Heavy Flavor Transport** in QCD Matter Part IV 5*LO-pQCD Langevin & **RRM vs instantaneous coalescence Min He** Nanjing University of Sci. & Tech.

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GSI-HF-RRTF, follow-up meeting, Dec.12,2016

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Charm quark relaxation rate: 5*LO-pQCD



low T: T-matrix > 5*LO-pQCD, high T: T-matrix < 5*LO-pQCD
 very similar momentum dependence

Charm quark relaxation rate: comparison



- bands: T-matrix, 20% uncertainty due to different IQCD input potential
- thin lines: LO-pQCD with alpha_s=0.4
- thick lines: Nantes (pQCD Born with reduced screening mass & running coupling

Calibrating bulk medium



• p_T spectra & integrated <v₂> of charged particles fitted at thermal freezeout T_{kin}=110 MeV

Bulk hadrons spectra vs v₂ at Tc=170 MeV



Post-point Langevin scheme

• Langevin equation

$$dx_{j} = \frac{p_{j}}{E}dt,$$

$$dp_{j} = -\Gamma(p,T)p_{j}dt + \sqrt{dt}C_{jk}(p + \xi d p,T)\rho_{k}$$

with
$$C_{jk}(p) = \sqrt{2B_0(p)}P_{jk}^{\perp}(p) + \sqrt{2B_1(p)}P_{jk}^{\parallel}(p)$$

• use 5*LO-pQCD transport coefficient:

$$\Gamma(p;T) = A(p;T) + \frac{1}{E(p)} \frac{\partial D(p;T)}{\partial E(p)}$$

 $= A(p) + \mathcal{O}(T/m_Q)$

--- Einstein relation between A(p,T) and longitudinal diffusion

 $B_1(p,T) = A(p,T)E(p)T$

--- A(p,T) & B₀(p,T) taken from LO-pQCD calculations

Charm quark FONLL fragmentation



- initial charm quark spectrum taken from FONLL
- hadronization other than recombination also consistently by FONLL frag. func.

Charm quark R_{AA} vs v₂



- \mathbf{R}_{AA} -- slight increase toward high \mathbf{p}_{T}
- v_2 --- drop down toward high p_T
- all similar to previous T-matrix results --- recall similar p-dependence in their A(p,T)

D-meson R_{AA} vs v₂

• low p_T, Resonance Recombination/RRM dominates; high p_T, fragmentation takes over



RRM vs instantaneous coalescence

Resonance Recombination

$$p^{\mu} \partial_{\mu} f_{M}(t, \vec{x}, \vec{p}) = -m\Gamma f_{M}(t, \vec{x}, \vec{p}) + p^{0}\beta(\vec{x}, \vec{p}),$$

$$\beta(\vec{x}, \vec{p}) = \int \frac{d^{3}p_{1}d^{3}p_{2}}{(2\pi)^{6}} f_{q}(\vec{x}, \vec{p}_{1}) f_{\bar{q}}(\vec{x}, \vec{p}_{2})$$

$$s \sigma(s) v_{rel}(\vec{p}_{1}, \vec{p}_{2}) \delta^{3}(\vec{p} - \vec{p}_{1} - \vec{p}_{2})$$
Breit-Wigner
$$\sigma(s) = g_{\sigma} \frac{4\pi}{k^{2}} \frac{(\Gamma m)^{2}}{(s - m^{2}) + (\Gamma m)^{2}}$$

→ resonance formation in the equilibrium limit (width from T-matrix)

$$f_M^{\rm eq}(\vec{p}) = \frac{E_M(\vec{p})}{m\Gamma} \int d^3x \beta(\vec{x}, \vec{p})$$

• Instantaneous coalescence Ko et al., 2003 & 2009

$$\frac{dN_M}{d^2 \vec{p}_T} = g_M \frac{(2\sqrt{\pi}\sigma)^3}{V} \int d^2 \vec{p}_{T1} d^2 \vec{p}_{T2} \frac{dN_1}{d^2 \vec{p}_{T1}} \frac{dN_2}{d^2 \vec{p}_{T2}} e^{-\vec{k}_T^2 \sigma^2} \delta^2 (\vec{p}_T - \vec{p}_{T1} - \vec{p}_{T2})$$

where $k = \frac{1}{m_1 + m_2} (m_2 p'_1 - m_1 p'_2)$

with a Gaussian Wigner function fitted to meson rms charge radius

D-meson: RRM vs Ko-coalescence

• different implementations:

- --- RRM: event-by-event coupled to Langevin, with full space-momentum correlation on the hydro freezeout hypersurface
- --- Ko-coalescence: done in momentum space only with "averaged" quark momentum distribution, thus no space-momentum correlation



Back-up: D-meson RRM equilibrium



- ullet charm quark Langevin with huge thermalization rate ullet reaching equilibrium
- then recombine them with hydro light quarks \rightarrow equilibrium D-meson spectrum